

*Regional Cooperation for
Limited Area Modeling in Central Europe*



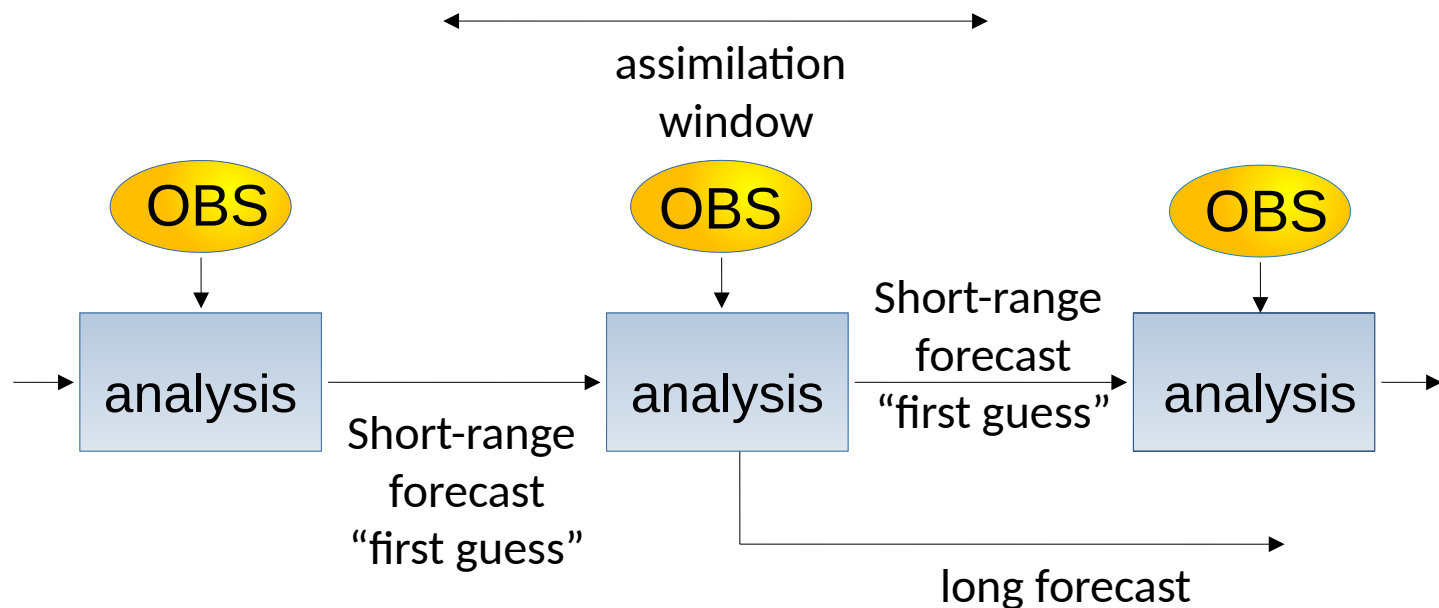
Diagnosics in data assimilation

Benedikt Strajnar



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- ▶ 2) Relative strength of obs. in analysis (DFS)
- ▶ 3) Relative impact of obs. on forecast (MTEN)
- ▶ 4) Covariances of residuals: tuning of DA



Why diagnostics?

- ▶ Data assimilation: combines “a priori” information with observations

$$J = (x - x_b)^T B^{-1} (x - x_b) + (y - H(x))^T R^{-1} (y - H(x))$$

- ▶ Ingredients: previous forecast, observations, data assimilation method, *statistical properties of errors*
- ▶ Aims of diagnostics in DA:
 - Validity of data assimilation method
 - Validity of assumptions about errors
 - Impact of (groups of) obs. on analysis and forecast
 - Statistical quality control of new observations

1) Analysis of DA residuals

- ▶ **OMG (fg_depar):** $y - H(x_b)$
 - Depends on quality of both first guess and observations
- ▶ **OMA (an_depar):** $y - H(x_a)$
 - Depends on DA method and its tuning, not a measure of quality
- ▶ **OMA < OMB** if assimilation converged
- ▶ **Mean OMA and OMG** are measures of systematic errors in the system (bias)

Residuals in DA

- ▶ Obtained by a simple ODB query

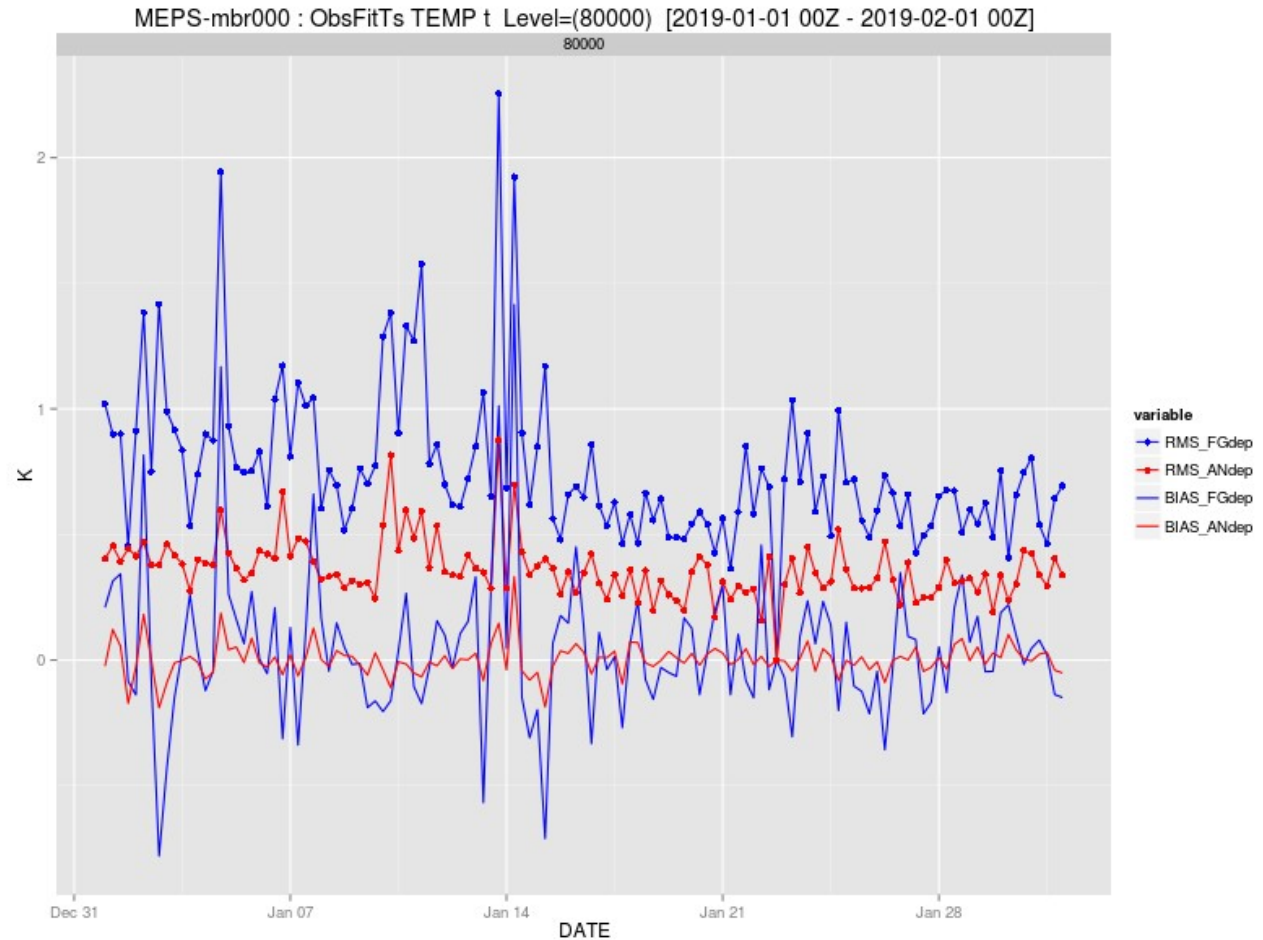
```
odbsql -q 'select an_depar, fg_depar, obsvalue  
from hdr, body'
```

from CCMA once minimization has finished

- ▶ ECMA: after screening, $an_depar = fg_depar$

Monitoring of active observations

- ▶ Does analysis reduce the OMG rms and bias?
- ▶ How close the analysis fits observations?

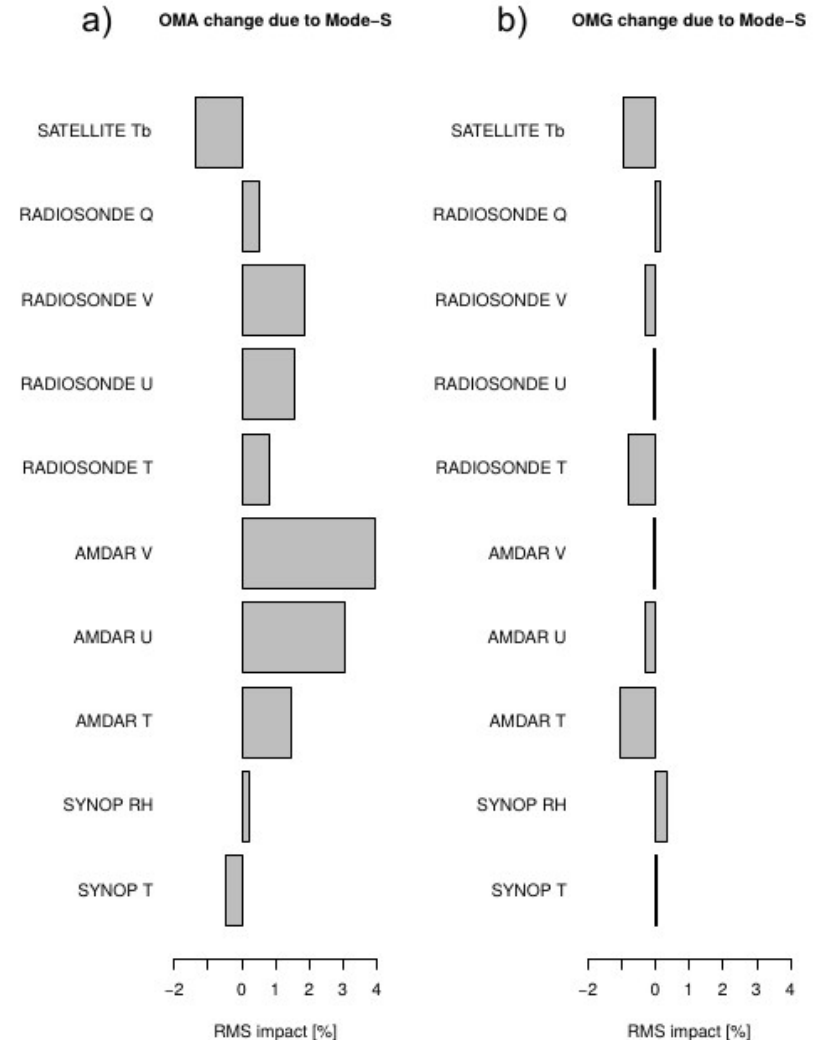


Residuals in active DA

- ▶ Relative change in OMA and OMG for a new observation set tells us about its impact.

Left: Relative change of OMA because of assimilated new observations

Right: Relative change of OMG because of assimilated new observations

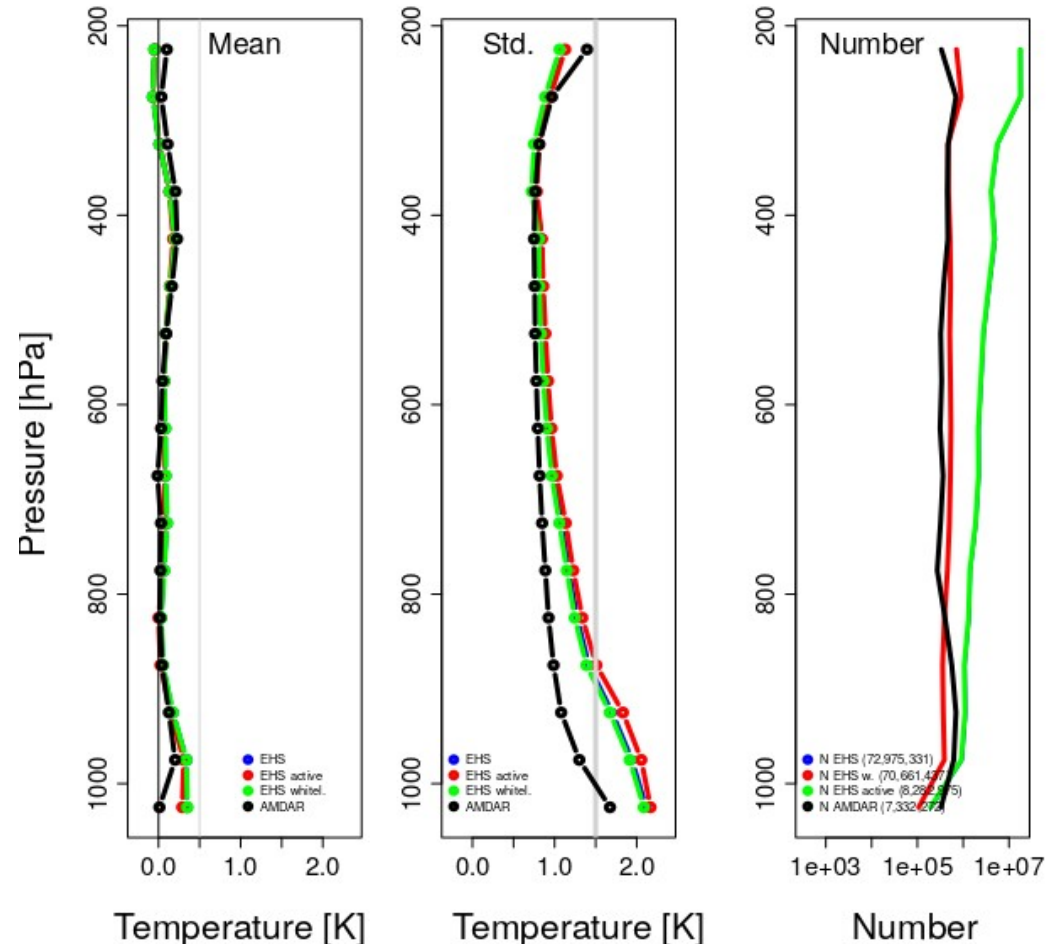


Passive monitoring in DA – example 1

- ▶ If OMG is accumulated over long time for different observations, its relative quality can be estimated

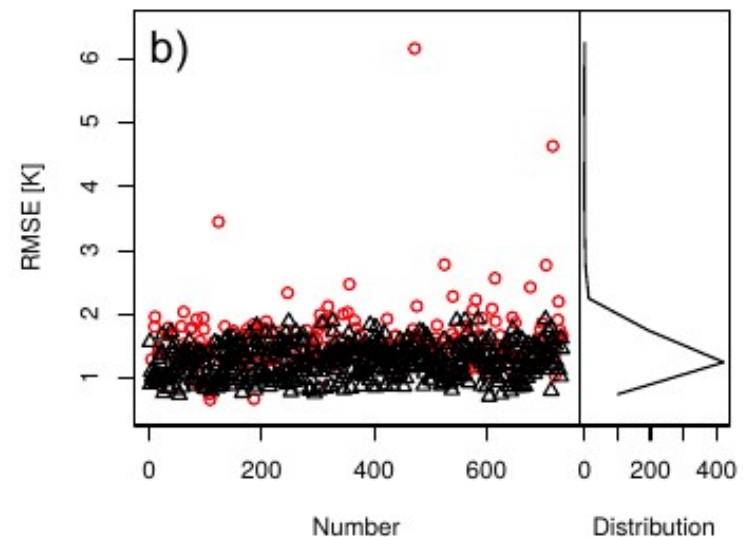
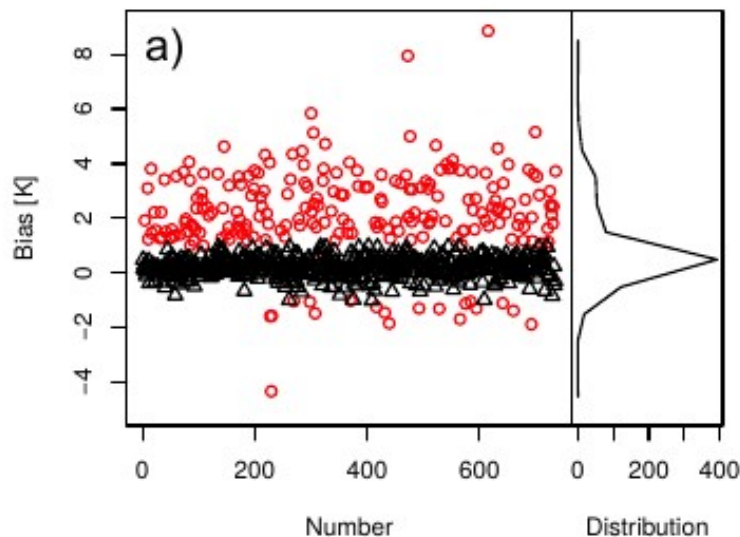
Mean and std. of passive OMG for different aircraft observation groups

Profile of T aircraft OMG departures
Aircraft number EHS all:7012 whitelisted:4618 active:6880 AMDAR:1094 SI_MRAR:208
Size of EHS dataset reduced to 10%



Passive monitoring in DA – example 2

- ▶ Long term OMG can be used to detect erroneous observations (instrument errors) – beware of other errors contained in R!



Mean and std. of passive temperature **OMG** for different airplanes.

Degrees of freedom for signal (DFS)

- ▶ Question: What is the strength of i-th obs. group in analysis:

$$DFS_i = \sum_{y \in obs} \left(\frac{\partial H_i x_a}{\partial y_i} \right)$$

$$DFS_i = Tr(\mathbf{KH})_i$$

- ▶ As there is no explicit K in the variational assimilation, we apply „Monte Carlo“ approach

$$\partial y'^T \mathbf{HK} \partial y' = Tr(\mathbf{HK} y'^T \partial y') = Tr(\mathbf{HK})$$

Cardinali et al. (2004), Chapnik et al. (2006)

Degrees of freedom for signal (DFS)

- ▶ If one sets

$$y' = y + \mathbf{R}^{1/2} \partial y'$$

the trace can be computed by two analyses x_a, x'_a
using y, y' observation sets.

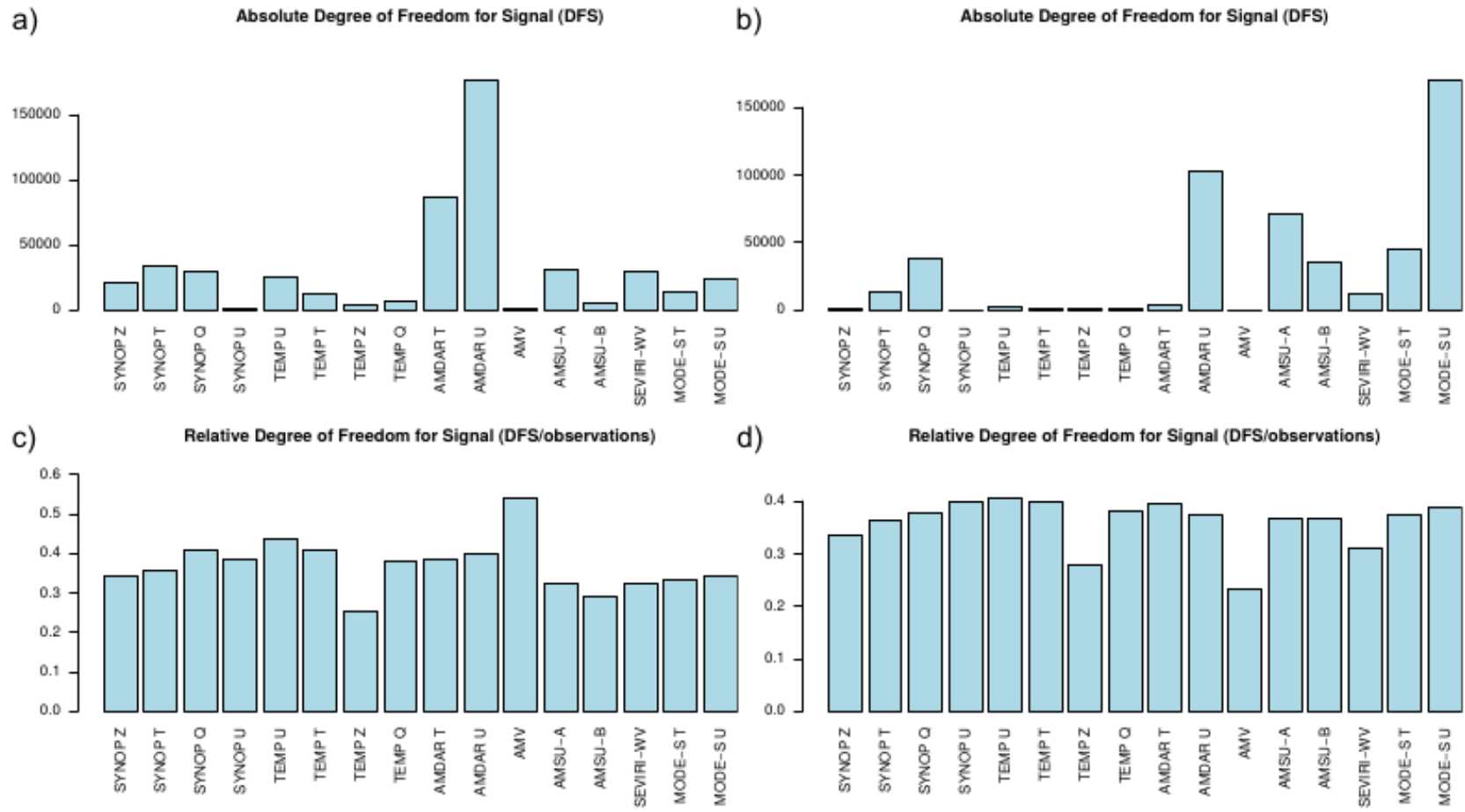
$$\text{Tr}(\mathbf{KH}) = (y' - y) \mathbf{R}^{-1} \mathbf{H}(x'_a - x_a)$$

- ▶ By applying to what is available from the ODB we get:

$$\text{DFS} = (\text{OMG}' - \text{OMG})^T \mathbf{R}^{-1} (\text{OMA}' - \text{OMA})$$

- ▶ DFS can then be computed by observation groups.

DFS - interpretation



DFS- how to perturb observations?

► Program PERTCMA:

- Copy/duplicate the existing unperturbed CCMA

```
{mpirexec} ./PERTCMA -N CCMA
```

- N is seed for random number generator (int)
- Adds perturbations with zero mean and sigma = $\sqrt{\mathbf{R}}$ to all observations
- Can also be executed inline in screening
 - NAMSCC: LPERTURB=T

DFS - computation?

- ▶ Predefined query to ODB:

```
odbsql -q 'select obstype, codetype, statid, varno, vertco_reference_1,  
degrees(lat), degrees(lon), an_depar, tdiff(date,time,an_date,an_time)/60, fg_depar,  
obsvalue from hdr,desc,body where varno/=91 and an_depar/="NULL" and  
obstype/=7' | grep -v obsvalue
```

- ▶ Program dfscomp (by A. Storto)

```
./dfstot.x pert_CCMA unpert_CCMA
```

- ▶ Can be then aggregated over the period, variable, observation group etc.

2. Moist total energy norm (MTEN)

- Measures strength of influence of observation group on forecast

$$J^i(t) = \langle x_t^i - x_t^{ctrl}, x_t^i - x_t^{ctrl} \rangle$$

Where J is an arbitrary norm.

- MTEN norm combines all main meteorological variables:

$$J_i = \int_{p_0}^{p_1} \int_D (u^2 + v^2 + \frac{c_p}{T_r} T^2 + \frac{RT_r}{p_r^2} p^2 + \frac{L^2}{c_p T_r} q^2) \frac{\partial p_r}{\partial p} dp dD$$

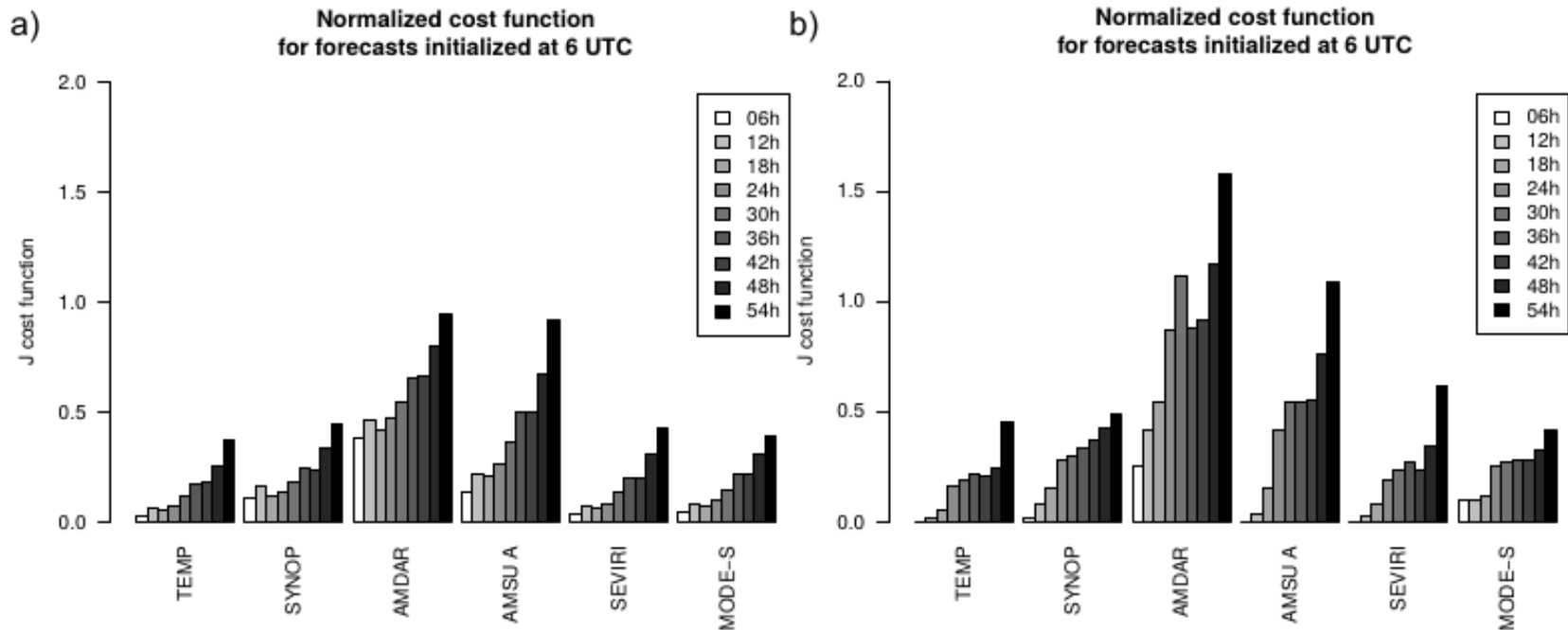
A. Storto, R. Randriamampianina (2010)

MTEN - computation

- Package on the LACE forum:
<http://www.rclace.eu/forum/viewtopic.php?f=21&t=375&p=1564&hilit=mten#p1564>
- A special executable needs to be compiled by replacing some of the model source routines and entry point
- The analysis step is repeated several times, each time one observation is omitted
- Additional sets of forecasts are generated, history files are saved
- MTEN uses history files (control and the one with omitted observations) to compute the norms.

Moist total energy norm (MTEN)

- Shows relative importance of observations over time



4) Covariances of residuals

- Linear estimation theory: $\mathbf{K} = \mathbf{B}\mathbf{H}^T(\mathbf{H}\mathbf{B}\mathbf{H}^T + \mathbf{R})^{-1}$
- From the definition of background departure:

$$\text{OMG} = y - \mathbf{H}(x_b) = y - \mathbf{H}(x_t) + \mathbf{H}(x_t) - \mathbf{H}(x_b) \simeq \epsilon_o - \mathbf{H}\epsilon_b$$
- Taking the expectation operator and assuming that **R** and **B** are not mutually correlated:

$$\begin{aligned} E[\text{OMG}(\text{OMG}^T)] &= E[\epsilon_o\epsilon_o^T] - E[\epsilon_o\epsilon_b^T]\mathbf{H}^T + \mathbf{H}E[\epsilon_b\epsilon_o^T] + \mathbf{H}E[\epsilon_b\epsilon_b^T]\mathbf{H}^T \\ &= E[\epsilon_o\epsilon_o^T] + \mathbf{H}E[\epsilon_b\epsilon_b^T]\mathbf{H}^T \\ &= \mathbf{R} + \mathbf{H}\mathbf{B}\mathbf{H}^T \end{aligned}$$

Desroziers et al., 2005

4) Covariances of residuals

- Similar derivation, using the residuals

$$OMG = y - H(x)$$

$$AMG = H(x_a) - H(x_b) = \mathbf{H}\partial x_a$$

$$OMA = y - H(x_a)$$

leads to further relations:

$$E[OMG(OMG)^T] = \mathbf{HBH}^T + \mathbf{R}$$

$$E[AMG(OMG)^T] = \mathbf{HBH}^T$$

$$E[OMA(OMG)^T] = \mathbf{R}$$

$$E[AMG(OMA)^T] = \mathbf{HAH}^T$$

Hollingsworth & Lonnerberg method

- Based on covariances of OMG departures, binned by distance between observations
- **B** and **R** are separated by assuming no spatial correlation in **R** and by extrapolating OMG covariance to 0.

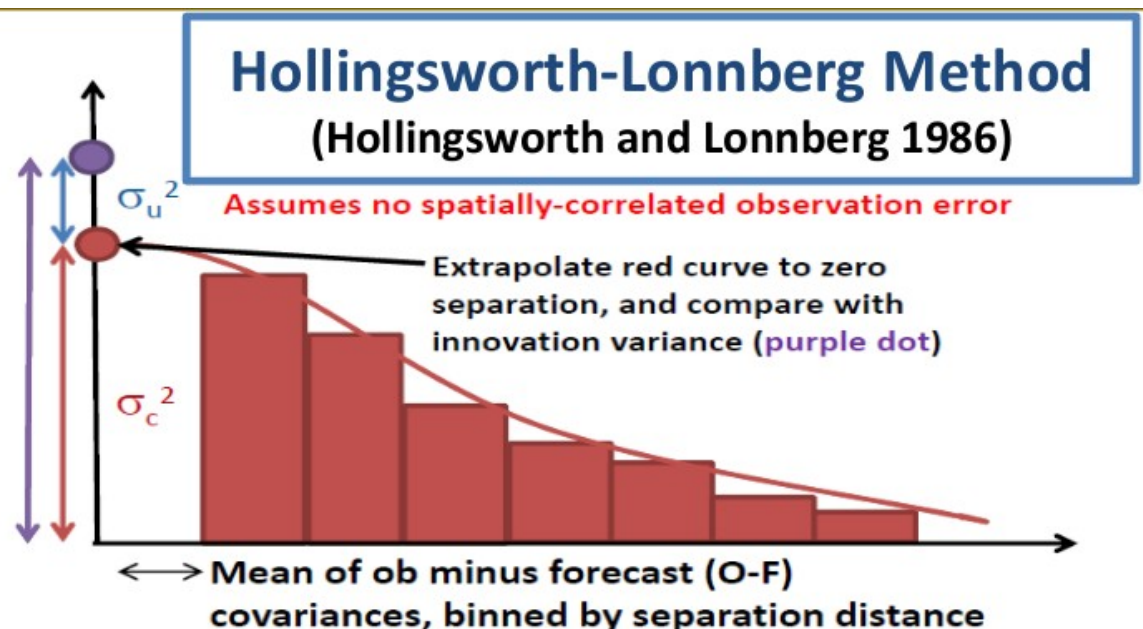


Figure by
Campbell and
Satterfield, NRL

A-posteriori tuning of **R** and **B**

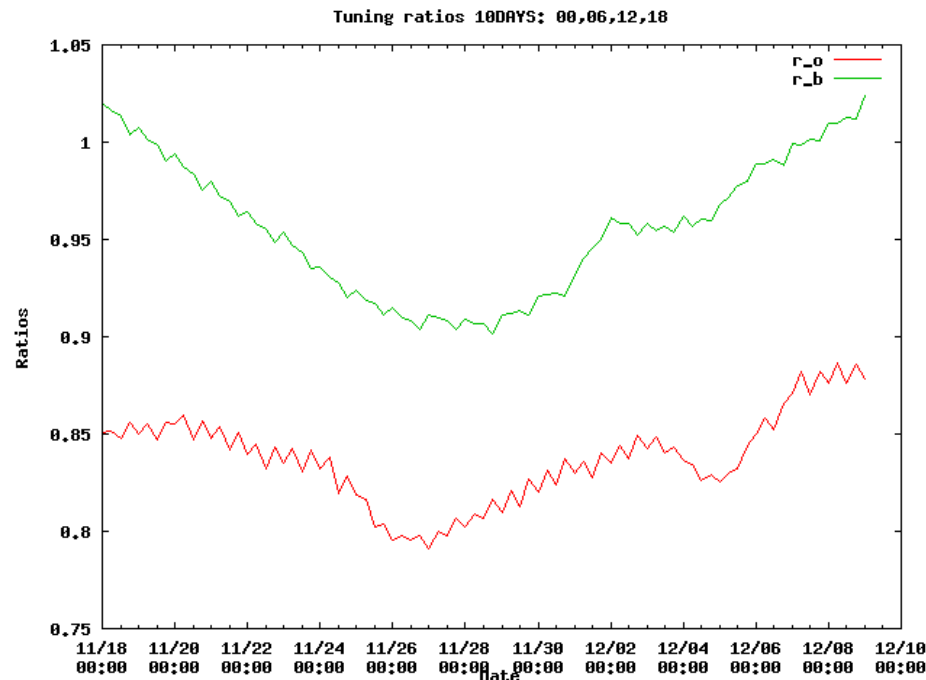
- The diagnosis is possible for any observation subset.
- If the diagnosed R and B are not in agreement with the predefined ones, we can use this method to tune them by *REDNMC* and *SIGMAO_COEFF*

$$B' = s B$$

- Covariances/correlations can be diagnosed (ObsTool in practicals).
- Tuning is an iterative process.

A-posteriori tuning of **R** and **B**

- Based on the ratio between predefined and diagnosed observation and background errors.
- Check impact on forecast as well!



Software for DA tuning

- Tune BR (G. Boloni)
 - <http://www.rclace.eu/forum/viewtopic.php?f=30&t=248&hilit=TuneBR>
 - Determines tuning factors for σ_o, σ_b
- OBSTool (P. Benacek)
 - Focuses on correlations in **B** (Desroziers and Hollingsworth&Lonnberg method) and **R**

Conclusions

- Diagnostic methods provide useful insights into assimilation regularity
- Enables tuning to reach more realistic balance between observations and first guess
- Typically influenced by many factors and depend on conditions which are not always met.
- Each diagnostic methods only focuses on a particular property of obs. impact.

Exercises

Exercise 1: DFS

- Run PERTOBS on the provided experiments.
- Preparation of perturbed CCMA ODB database
 - 1.1) Run the script `scr/prep_perturbed_ccma.sh`

```
qsub scr/prep_perturbed_ccma.sh
```

This perturbs the original ODB database for 4 different cases.

Exercise 1: DFS

- Check the perturbed ODB and compare it with the unperturbed one
module load odb
odbsql -q "select obsvalue from hdr,body where obstype=1 and varno=39" -o dump_perturbed.dat
- Exercise: Check that the perturbations really follow the Gaussian distribution with $\sigma = \sqrt{R}$.

Exercise 1: DFS

- Run the DFS computation from the precomputed perturbed and unperturbed analysis departures.

```
./run.sh
```

- Check the outputs in results subdirectory and run the plotting script

```
Rscript visualize_dfstot.R
```

```
Rscript time_evolution
```

- Check the plots by using eog and display.

Exercise 1: DFS

- What is the main difference between the two experiments?
- Which obs. types and variables have the greatest impact on the analysis?
- Which obs. types are the most valuable for the analysis?

Exercise 2: ObsTool

- * Modify the DFS computation program in src/dfscomp.F90 in order to compute the total DFS for conventional (SYNOP,AMDAR,TEMP) and remote-sensed observations (AMSU,IASI,SCATT,AMV,..). Which observations have bigger impact and which are more valuable in the analysis?

Run the DFS computation from the precomputed perturbed and unperturbed analysis departures.

```
cd scr  
./run.sh
```

2.1) Check the outputs in results subdirectory and run the plotting script

```
module load R  
Rscript visualize_dfstot.R  
Rscript time_evolution.R
```

Check the plots dfs_plot_total.ps, dfs_evolution_`\${EXPNAME}`.png.

Exercise 2: ObsTool

- Run the obs. tool on experiment aos, period 2018080100 - 2018081006, analysis every 3 hour.
- You don't need to extract ODBs as this is done in advance.
- Examine the generated plots for SYNOP, AMDAR and TEMP.
- Determine the optimal thinning distance for AMDAR and SYNOP which needs to be applied if R is considered as spatially uncorrelated (usually we are safe at distance where correlation falls below 0.2).

Exercise 1: DFS

- Run PERTOBS on the files
- Use odbselect to read aircraft data and check that the observations were properly perturbed.
- 1. Preparation of perturbed CCMA ODB database
 -
 - 1.1) Run the script `scr/prep_perturbed_ccma.sh`
 -
 - `qsub scr/prep_perturbed_ccma.sh`
 -

Exercise 3: ObsTool

- Run PERTOBS on the files
- Use odbselect to read aircraft data and check that the observations were properly perturbed.

